

## Abstract

- ▶ We present a framework for characterizing phase space transport, based on the theory of Phase Space Zonal Structures (PSZS) [1–5].
- ▶ We broaden the usual definition of plasma equilibrium in the presence of a finite level of electromagnetic fluctuations, i.e., the Zonal State (ZS).
- ▶ We introduce a subcycling approach that captures the dynamics of the ZS over transport time scales consistent with different levels of reduced dynamics.
- ▶ We compare PSZS evolution across nonlinear GK simulations, including HMGC [6], GTC [7], and XTOR-K [8], to benchmark nonlinear dynamics across different GK codes.
- ▶ We also compare GK results with the ATEP workflow [3] to verify the reduced transport approach adopted in ATEP.

## Background

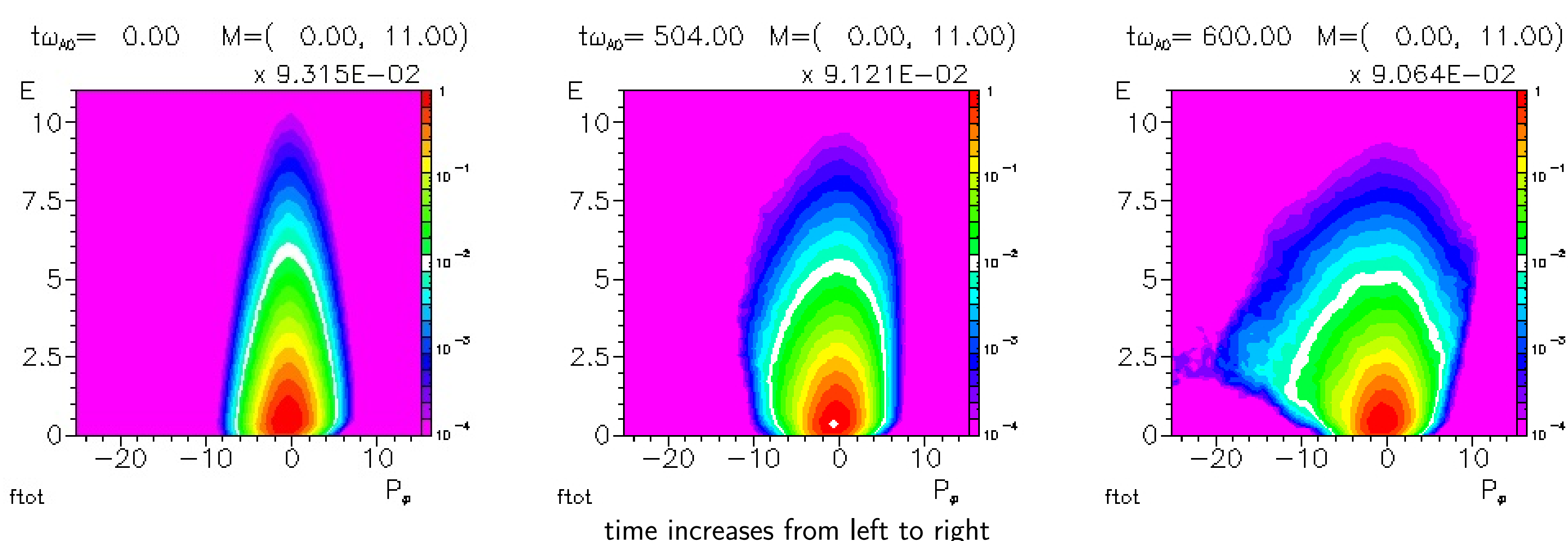
- ▶ Predicting the dynamics of a burning plasma over long time scales, comparable with the energy confinement time or even longer, is crucial for understanding next generation fusion experiments.
- ▶ The majority of studies on core plasma transport rely on a systematic separation of scales between the reference equilibrium and fluctuations.
- ▶ Energetic particle transport in fusion devices is a spatiotemporal multi-scale process.
- ▶ Spatio-temporal mesoscales can be observed even in drift wave plasma turbulence simulations [9].
- ▶ Recent work [5] emphasized the importance of a self-consistent determination of the characteristic spatiotemporal scales of the reference state.

## Phase Space Zonal Structures (PSZS)

- ▶ PSZS equation is connected with the macro-meso-scopic component of the unperturbed orbit-averaged distribution function.  

$$\frac{\partial \bar{F}_0^{(0)}}{\partial t} + \frac{1}{\tau_b} \left[ \frac{\partial}{\partial P_\phi} (\tau_b \delta \dot{P}_\phi \delta F)_z^{(0)} + \frac{\partial}{\partial \mathcal{E}} (\tau_b \delta \dot{\mathcal{E}} \delta F)_z^{(0)} \right]_S = \bar{C}_S^{(0)} + \bar{S}_S^{(0)}$$
- ▶ By construction, PSZS evolves only through collisions, sources, and nonlinear phase-space fluxes.
- ▶ Fast collisionless oscillations are filtered out of  $\bar{F}_0^{(0)}$ , making it a natural renormalized equilibrium for burning-plasma transport.
- ▶ The toroidally symmetric distribution function can be decomposed so that micro-scales are accounted for separately, while macro- and meso-scales are described by PSZS.
- ▶ The evolution of the PSZS during an EPM, obtained with HMGC [6], is shown below.

$$F_z = \bar{F}_z^{(0)} + \delta \bar{F}_z = \bar{F}_0^{(0)} + \delta \bar{F}_z^{(0)} + \delta \bar{F}_z$$



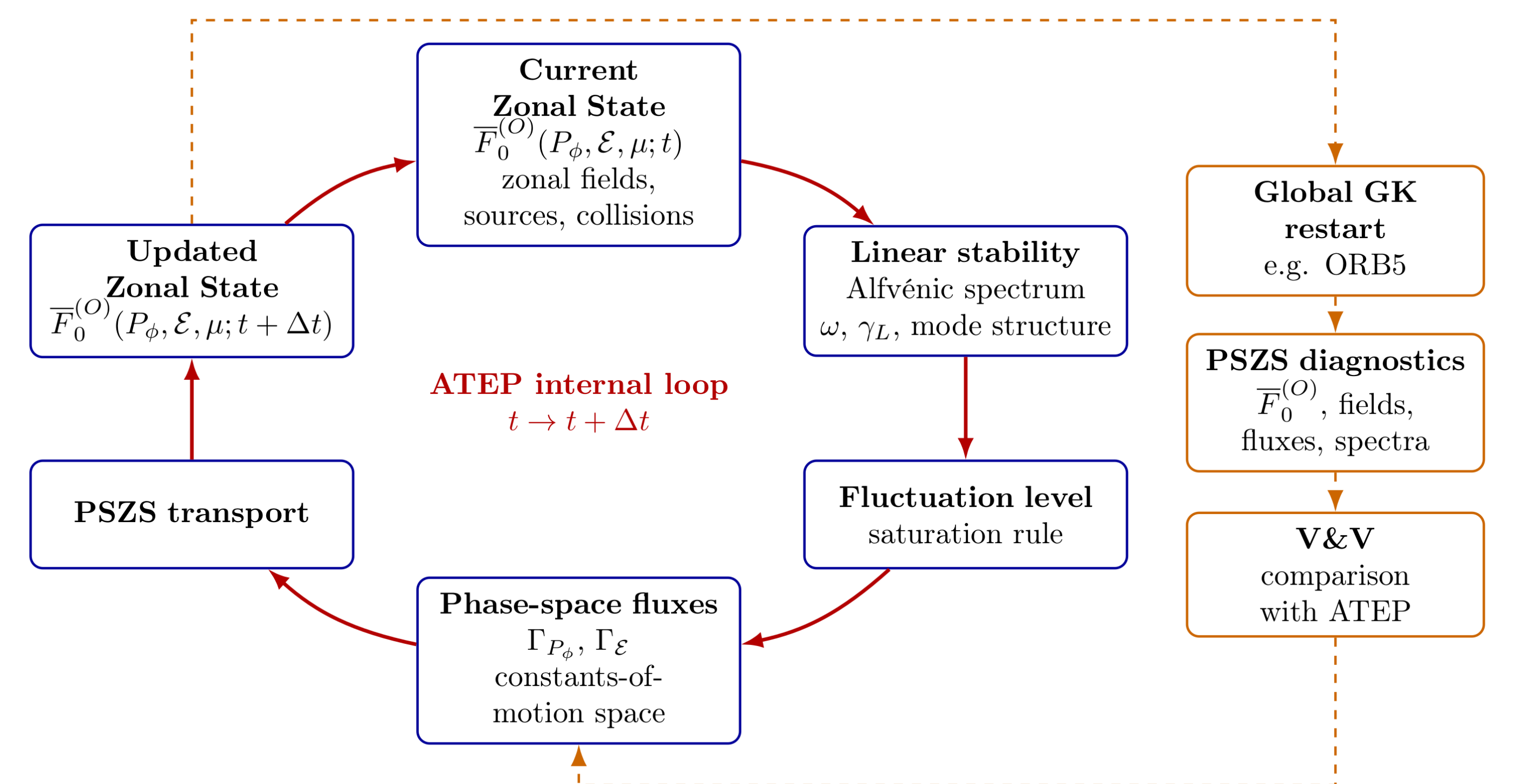
## Acknowledgements / References

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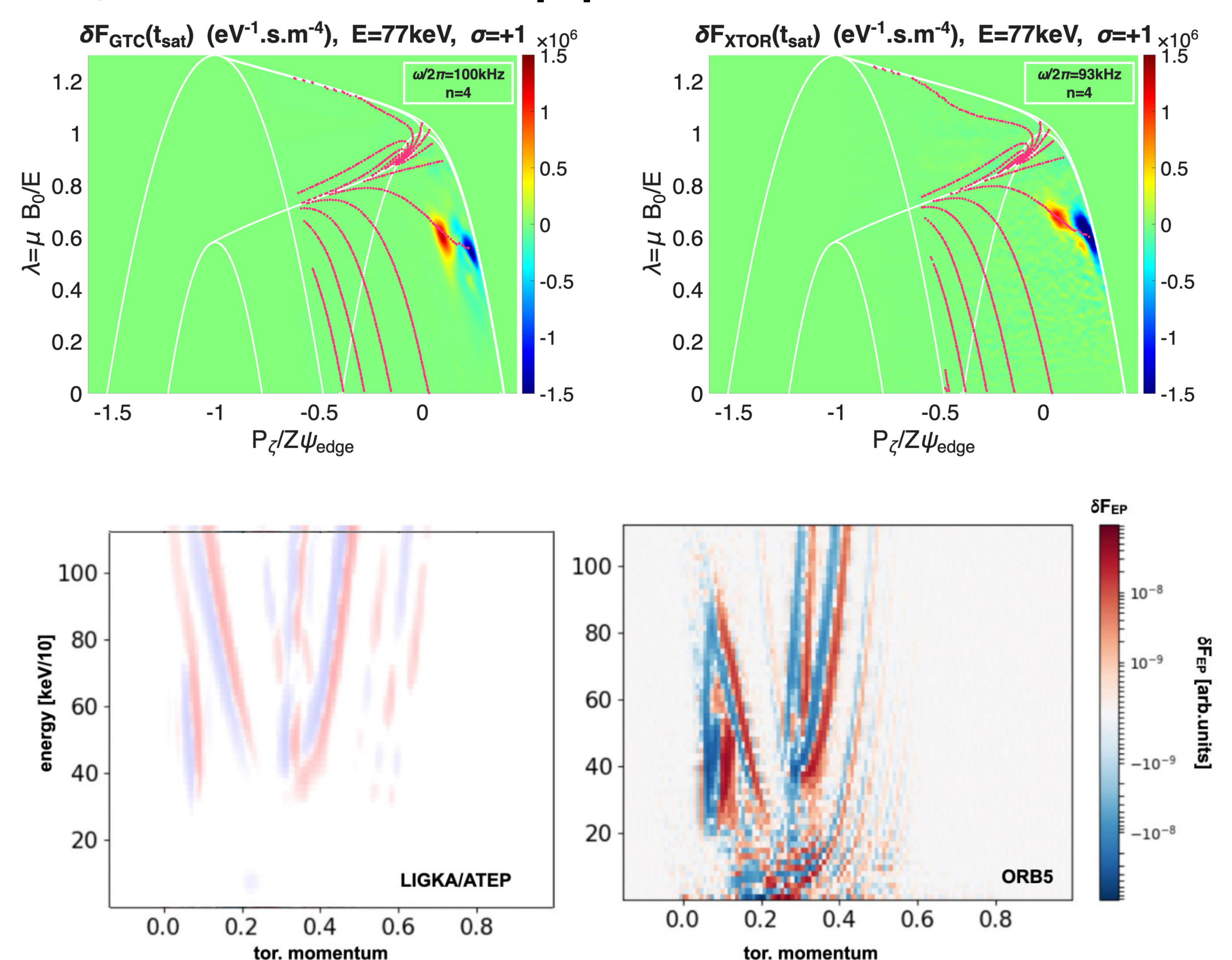
## Hierarchical Transport

- ▶ Highest-fidelity level: fully nonlinear global GK evolves the complete Zonal State and provides the natural verification target.
- ▶ Intermediate level: reduced nonlinear envelope or Dyson-Schrodinger dynamics retains coherent mesoscopic and nonlocal effects when  $|\gamma_L| \sim \tau_{NL}^{-1} \ll |\omega|$  [5,10].
- ▶ Reduced-transport level: quasi-linear, mixing-length, or saturation-rule closures evolve the PSZS over transport time scales with sources and collisions.
- ▶ ATEP provides a common workflow in which the same Zonal-State evolution is advanced using different reduced models, while global GK simulations provide the verification target [11,12].



## PSZS Benchmarks

- ▶ The reduced ATEP evolution can be compared directly with PSZS diagnostics extracted from global GK simulations, providing a systematic route for verification of reduced models [13].
- ▶ A successful benchmark is performed for BAE-induced PSZS in a DIII-D plasma [14] using GTC and XTOR-K, with realistic beam-distribution input from the EPCoM code [15].



## Conclusion

- ▶ We introduced the concept of zonal state to describe the evolution of the plasma between neighboring nonlinear equilibria.
- ▶ The framework provides a scheme to study transport processes in burning plasmas.
- ▶ The evolution of the zonal state has been studied by means of nonlinear GK simulations.
- ▶ Reduced transport models are verified within the same framework.