

Expanding ASTRA: A unified framework for tokamak and stellarator transport modelling



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INTRODUCTION / MOTIVATION

Fenix flight simulator [1]:

- Simulates entire discharges using ASTRA transport solver [2,3] to model the plasma and a simulated control system in the framework of PCSSP (Plasma Control System Simulation Platform) [4]

→ Development of the first stellarator flight simulator

- Reduced models and current diffusion equation in ASTRA were initially derived for tokamaks

Extension of ASTRA8 code to stellarator physics:

- Implementation of a generic current diffusion equation [5]

- Coupling to a 3D equilibrium solver [5,6]

- Calculation of neoclassical transport and bootstrap current in 3D geometry [7]

UPGRADING ASTRA8 FOR STELLARATORS [5,6,7]

Upgraded current diffusion equation [5]:

$$\frac{\partial \Psi}{\partial t} \Big|_{\rho} = \frac{2\pi B_0 \rho}{\sigma_{\parallel} \mu_0} (S_{21} \iota + S_{22})^2 \frac{\partial}{\partial \rho} \left[\frac{1}{S_{21} \iota + S_{22}} \left(\frac{S_{11}}{2\pi B_0 \rho} \frac{\partial \Psi}{\partial \rho} + S_{12} \right) \right] - \frac{V'}{2\pi \rho \sigma_{\parallel}} (j_{BS} + j_{CD})$$

→ Valid for both stellarators and tokamaks (S_{12} and S_{21} are only nonzero for nonaxisymmetric devices)

→ Ψ is the poloidal magnetic flux, $\iota \equiv \partial \Psi / \partial \Phi$ is the rotational transform

→ S_{ij} are 3D geometrical factors as defined in [5]

- Robin boundary condition based on external circuit equation:

$$U_{\text{ext}} = U_{\text{pl}}(\rho_B) + \frac{d}{dt} (L_{\text{ext}} I_{\text{tor}})$$

$$\Leftrightarrow \Psi(\rho_B) + L_{\text{ext}} \frac{S_{11}(\rho_B)}{\mu_0} \frac{\partial \Psi}{\partial \rho} \Big|_{\rho_B} = \Psi_{\text{ext}} + \frac{2\pi B_0 \rho_B}{\mu_0} L_{\text{ext}} S_{11}(\rho_B) \iota_{\text{vac}}(\rho_B)$$

Furthermore:

- Coupling to the **3D equilibrium solver VMEC** [8] to ensure a self-consistent evolution of the equilibrium [5,6]

- Coupling to **DKES** [9] via look-up tables to enable the calculation of **neoclassical transport coefficients** and the **bootstrap current**, and the evolution of the **radial electric field** [7]

VALIDATION AGAINST A W7-X DISCHARGE

- Simulation of W7-X discharge 20171206.036

- n_e and T_e profiles are taken from the experiment

- ECCD current density calculated using TRAVIS [10]

Two cases:

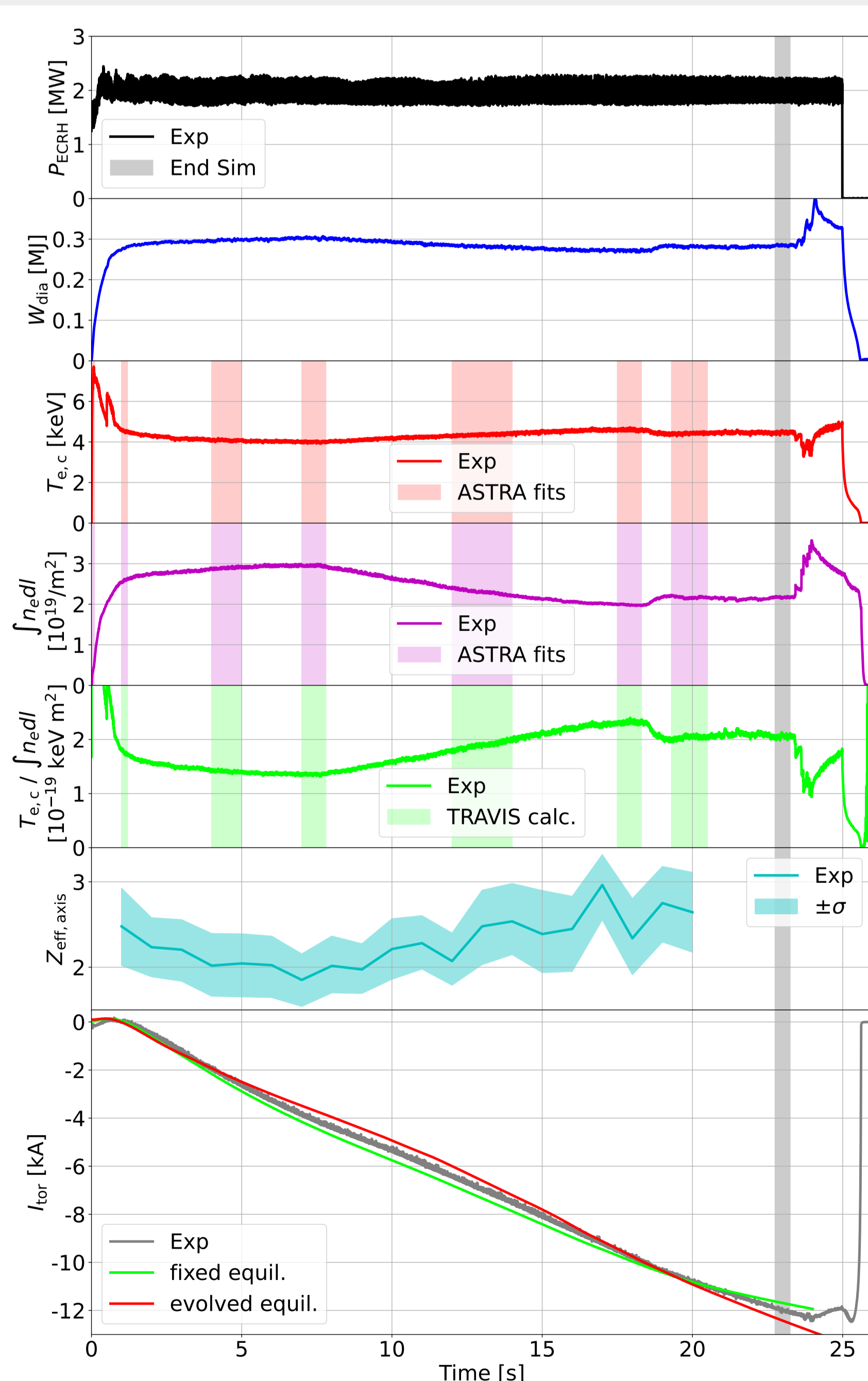
1. As in [5]: fixed equilibrium; σ_{\parallel} calculated using the expression from [11]; bootstrap current approximated using a parabolic profile with a total current of 2.5 kA

2. Evolved equilibrium; σ_{\parallel} and bootstrap current calculated as in [7]

→ In both cases, the simulated total toroidal current matches the experimental evolution

→ Remaining deviations can easily be explained by error bars in n_e , T_e , and Z_{eff} profiles

→ Difference between the case with fixed equilibrium and the case with self-consistent equilibrium evolution can be observed, but the overall behaviour of the current evolution remains unchanged



SUMMARY / OUTLOOK

- Validation of the generic current diffusion equation with self-consistent calculation of the equilibrium [6], and computation of parallel conductivity and bootstrap current for stellarators [7]

→ Evolution of the total toroidal current matches the experiment

- Investigation of the dynamic response of stellarator current profiles to modulated current drive

→ Local and global current evolution occur on different timescales

→ Self-consistent evolution of the equilibrium transforms the linear response of oscillatory current drive into a nonlinear dynamical evolution, generating additional frequency components through feedback between current diffusion and equilibrium evolution

NONLINEAR CURRENT RESPONSE

Oscillatory ECCD:

- T_e , n_e , and Z_{eff} taken from W7-X discharge 20171206.036 at 7.8 s

- Calculation of bootstrap current using DKES coupling described in [7]

- ECCD:

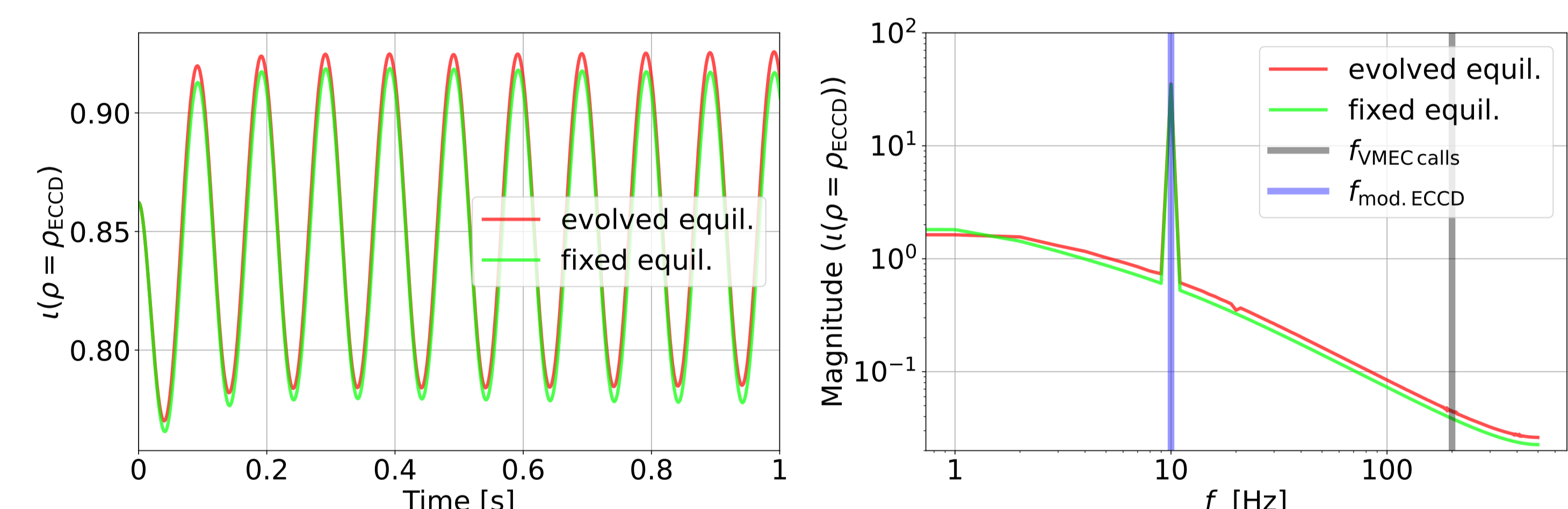
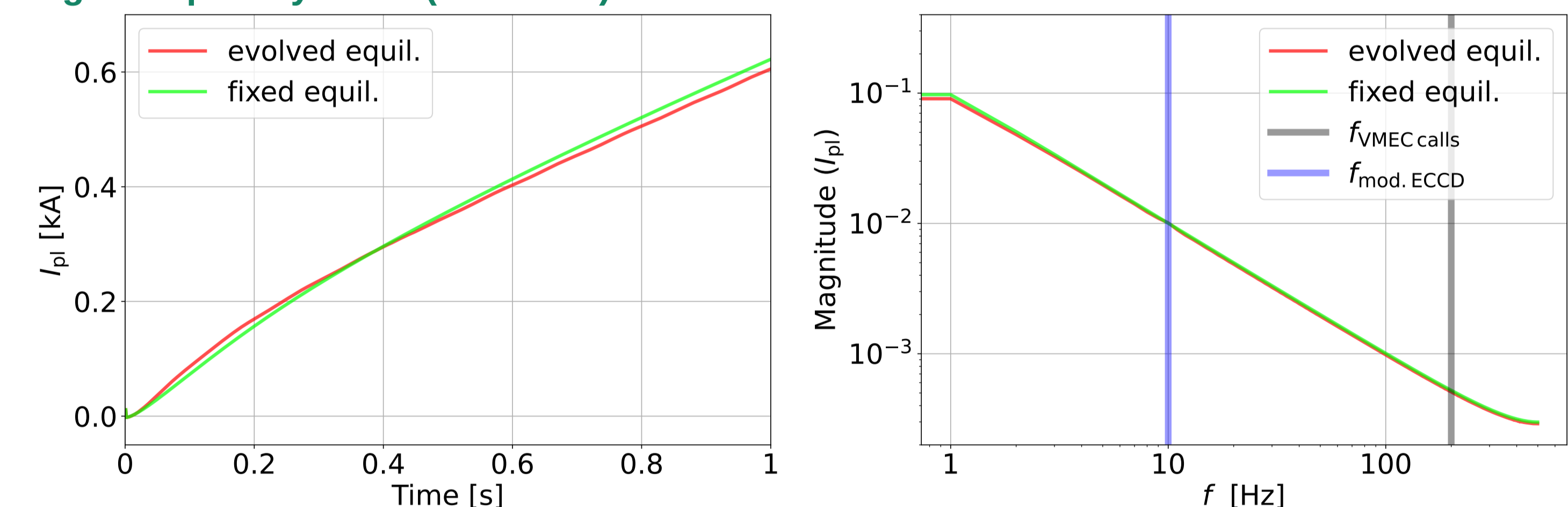
$$j_{\text{ECCD}}(t) = \sin\left(\frac{2\pi}{T}t\right) j_{\text{ECCD},t=7.8\text{s}}$$

Comparison:

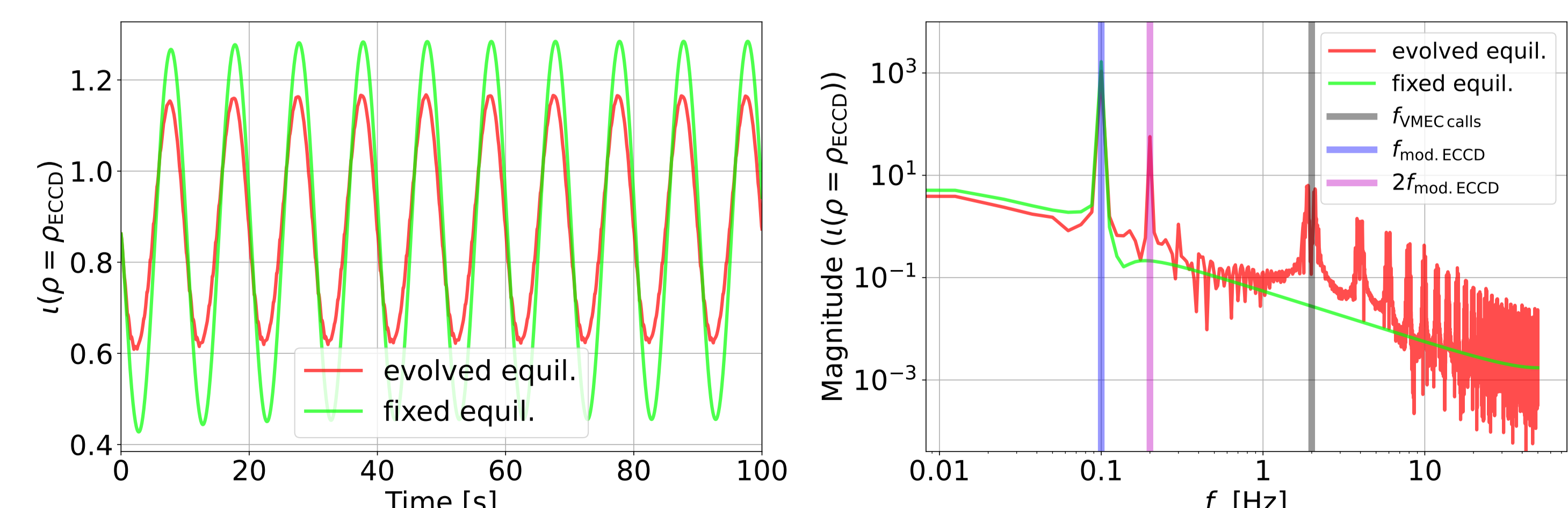
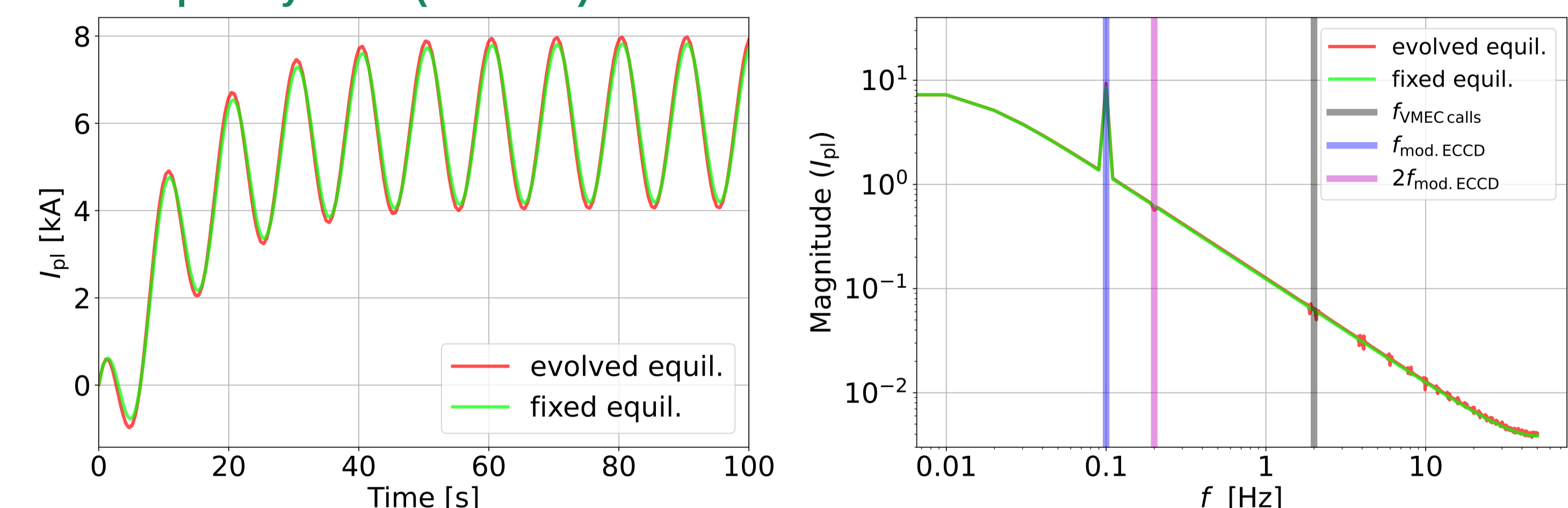
1. Low vs. high frequency ($T_1 = 0.1$ s; $T_2 = 10$ s)

2. Fixed vs. self-consistently evolved equilibrium

High frequency case ($T = 0.1$ s):



Low frequency case ($T = 10$ s):



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[10] N. B. Marushchenko *et al* 2014 *Comput. Phys. Commun.* **185** 165–76

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